

UNIQUENESS OF E_∞ STRUCTURES FOR CONNECTIVE COVERS

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ABSTRACT. We refine our earlier work on the existence and uniqueness of E_∞ structures on K -theoretic spectra to show that at each prime p , the connective Adams summand ℓ has an essentially unique structure as a commutative \mathbb{S} -algebra. For the p -completion ℓ_p we show that the McClure-Staffeldt model for ℓ_p is equivalent as an E_∞ ring spectrum to the connective cover of the periodic Adams summand L_p . We establish Bousfield equivalence between the connective cover of the Lubin-Tate spectrum E_n and $BP\langle n \rangle$ and propose $c(E_n)$ as an E_∞ approximation to the latter.

INTRODUCTION

The aim of this short note is to establish the uniqueness of E_∞ structures on connective covers of certain periodic commutative \mathbb{S} -algebras E . It is clear that the connective cover of an E_∞ ring spectrum inherits an E_∞ structure, but it is not obvious in general that this E_∞ multiplication is unique.

Our main concern are examples in the vicinity of K -theory; we apply our uniqueness theorem to real and complex K -theory and their localizations and completions and to the Adams summand and its completion.

The existence and uniqueness of E_∞ structures on the periodic spectra KU , KO and L was established in [5] by means of the obstruction theory for E_∞ structures developed by Goerss-Hopkins [8] and Robinson [12]. Note however, that obstruction theoretic methods would fail in the connective cases. Let e be a commutative ring spectrum. The obstruction groups for E_∞ multiplications consist of André-Quillen cohomology groups in the context of differential graded E_∞ -algebras applied to the graded commutative e_* -algebra e_*e . The algebra structures of ku_*ku , ko_*ko and $\ell_*\ell$ are far from being étale and therefore one would obtain non-trivial obstruction groups. One would then have to identify actual obstruction classes in these obstruction groups in order to establish the uniqueness of the given E_∞ structure – but at the moment, this seems to be an intractable problem. Thus an alternative approach is called for.

In Theorem 1.2 we prove that a unique E_∞ structure on E gives rise to a unique structure on the connective cover if E is obtained from some connective spectrum via a process of Bousfield localization. In particular, we identify the E_∞ structure on the p -completed connective Adams summand ℓ_p provided by McClure and Staffeldt in [10] with the one that arises by taking the unique E_∞ structure on the periodic Adams summand $L = E(1)$ developed in [5] and taking its connective cover.

Our Theorem applies as well to the connective covers of the Lubin-Tate spectra E_n and we prove in section 2 that these spectra are Bousfield equivalent to the truncated Brown-Peterson spectra $BP\langle n \rangle$. Unlike other spectra that are Bousfield equivalent to $BP\langle n \rangle$, such as the connective cover of the completed Johnson-Wilson spectrum, $\widehat{E}\langle n \rangle$, the connective cover of E_n is computationally convenient. So far, only $BP\langle 1 \rangle = \ell$ is known to have an E_∞ structure, and we propose the connective cover of E_n as an E_∞ approximation of $BP\langle n \rangle$.

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Let us first make explicit what we mean by uniqueness of E_∞ -structures.

Definition 1.1. In the following, we will say that an E_∞ -structure on some homotopy commutative and associative ring spectrum E is unique if whenever there is a map of ring spectra from some other E_∞ ring spectrum $\varphi: E' \rightarrow E$ which induces an isomorphism on homotopy groups, then there is a morphism in the homotopy category of E_∞ ring spectra $\varphi': E' \rightarrow E$ such that $\pi_*(\varphi) = \pi_*(\varphi')$.

If E and F are spectra whose E_∞ structure was provided by the obstruction theory of Goerss and Hopkins [8], then the Hurewicz map

$$(1.1) \quad \mathrm{Hom}_{E_\infty}(E, F) \xrightarrow{h} \mathrm{Hom}_{F_*\text{-alg}}(F_*E, F_*)$$

is an isomorphism. Assume that we have a mere ring map φ as above between E and F . This gives rise to a map of F_* -algebras from F_*E to F_* by composing $F_*(\varphi)$ with the multiplication μ in F_*F . The left hand side in (1.1) denotes the derived space of E_∞ -maps from E to F . In presence of a universal coefficient theorem we have $\mathrm{Hom}_{F_*\text{-hom}}(F_*E, F_*) = [E, F]$, therefore the element $\mu \circ F_*(\varphi)$ gives rise to a homotopy class of maps of ring spectra $\tilde{\varphi}$ from E to F . We can assume that we have functorial cofibrant replacement $Q(-)$, hence we obtain a ring map $Q(\tilde{\varphi})$ from $Q(E)$ to $Q(F)$. Via the isomorphism (1.1) this gives a map of E_∞ -spectra from $Q(E)$ to $Q(F)$, Φ , therefore we obtain a zigzag

$$\begin{array}{ccc} Q(E) & \xrightarrow{\Phi} & Q(F) \\ \vdots \sim & & \vdots \sim \\ E & \xrightarrow{\varphi} & F \end{array}$$

of weak equivalences of E_∞ spectra from E to F . Thus in such cases our definition agrees with the uniqueness notion that is natural in the Goerss-Hopkins setting.

Let E be a periodic commutative \mathbb{S} -algebra with periodicity element $v \in E_*$ of positive degree. We will view E as being obtained from a connective commutative \mathbb{S} -algebra e by Bousfield localization at $e[v^{-1}]$ in the category of e -modules. Let us denote the connective cover functor from [9, VII.3.2] by $c(-)$. For any E_∞ ring spectrum A , there is a weakly equivalent commutative \mathbb{S} -algebra $B(\mathbb{P}, \mathbb{P}, \mathbb{L})(A)$, with equivalence

$$\lambda: B(\mathbb{P}, \mathbb{P}, \mathbb{L})(A) \xrightarrow{\cong} A,$$

in the E_∞ category [7, XII.1.4]. Here $B(\mathbb{P}, \mathbb{P}, \mathbb{L})$ is a bar construction with respect to the monad associated to the linear isometries operad L and the monad for commutative monoids in the category of S -algebras \mathbb{P} . We will denote the composite $B(\mathbb{P}, \mathbb{P}, \mathbb{L}) \circ c$ by \bar{c} . For a commutative \mathbb{S} -algebra R and an R -module M , let $L_M^R(-)$ denote Bousfield localization at M in the category of R -modules and we denote the localization map by $\sigma: E \rightarrow L_M^R(E)$ for any R -module E .

Theorem 1.2. *Assume that we know that the E_∞ -structure on E is unique. Then there is a zigzag of E_∞ -equivalences between any other E_∞ -model e' of $c(E)$ and e .*

Proof. Each commutative \mathbb{S} -algebra can be viewed as an E_∞ ring spectrum. Let e' be a model for the connective cover $c(E)$, i.e., e' is an E_∞ ring spectrum with a map of ring spectra φ to $c(E)$, such that $\pi_*(\varphi)$ is an isomorphism. Write $v \in e'_*$ for the isomorphic image of v under $\pi_*(\varphi)^{-1}$. As φ is a ring map it will induce a ring map on the corresponding Bousfield localizations. But as the E_∞ -structure on E is unique by assumption, this map can be replaced by an equivalent equivalence, ξ , of E_∞ ring spectra. We abbreviate $B(\mathbb{P}, \mathbb{P}, \mathbb{L})(e')$ to $B(e')$. We consider the

following diagram whose dotted lines provide the required zigzag of E_∞ -equivalences.

$$\begin{array}{ccccc}
& & c(B(e')) & & c(e) \\
& \swarrow \varepsilon & \vdots & \searrow \varepsilon & \vdots \\
B(e') & \xrightarrow{\lambda} & e' & \xleftrightarrow{\sim} & e \\
\downarrow \sigma & & \downarrow c(\sigma) & & \downarrow c(\sigma) \\
L_{B(e')[v^{-1}]}^{B(e')} & \xrightarrow{\xi} & c(L_{B(e')[v^{-1}]}^{B(e')}) & \xrightarrow{c(\xi)} & c(E) \\
\downarrow \varepsilon & & \downarrow \varepsilon & & \downarrow \varepsilon \\
L_{B(e')[v^{-1}]}^{B(e')} & \xrightarrow{\xi} & E & & E
\end{array}$$

□

Real and complex K -theory, ko and ku , have E_∞ -structures obtained using algebraic K -theory models [9, VIII, §2]. The connective Adams summand ℓ has an E_∞ -structure because it is the connective cover of $E(1)$. In the following we will refer to these models as the standard ones. The E_∞ -structures on KO , KU and $E(1)$ are unique by [5, theorems 7.2, 6.2]. In all of these cases, the periodic versions are obtained by Bousfield localization [7, VIII.4.3].

Corollary 1.3. *Any E_∞ -structure on ko or ku , or on ℓ can be compared to the standard E_∞ -model by a zigzag of E_∞ -equivalences.*

In [10], McClure and Staffeldt construct a model for the p -completed connective Adams summand using algebraic K -theory of fields. Let $\tilde{\ell} = K(\mathbf{k}')$, the algebraic K -theory spectrum of $\mathbf{k}' = \bigcup_i \mathbb{F}_{q^{p^i}}$, where q is a prime which generates the p -adic units \mathbb{Z}_p^\times . Then the p -completion of $\tilde{\ell}$ is additively equivalent to the p -completed connective Adams summand ℓ_p [10, proposition 9.2]. For further details see also [2, §1]. An *a priori* different model for the p -completion of the connective Adams summand can be obtained by taking the connective cover of the p -complete periodic version $L = E(1)$. This is consistent with the statement of Corollary 1.3 because p -completion and Bousfield localization are compatible in the following sense. Consider $\ell = \bar{c}(L)$ and its p -completion

$$\lambda_\ell: \ell \longrightarrow \ell_p = (\bar{c}(L))_p.$$

The p -completion map λ is functorial in the spectrum, therefore the following diagram of solid arrows commutes.

$$\begin{array}{ccccc}
\ell = \bar{c}(L) & \xrightarrow{\lambda_\ell} & \ell_p = \bar{c}(L)_p & \xrightarrow{\dots} & \bar{c}(L_p) \\
\searrow & & \searrow & & \swarrow \\
L & \xrightarrow{\lambda_L} & L_p & & L_p
\end{array}$$

The universal property of the connective cover functor ensures that there is a map in the homotopy category of commutative \mathbb{S} -algebras from ℓ_p to $\bar{c}(L_p)$ which is a weak equivalence. In the following we will not distinguish ℓ_p from $\bar{c}(L_p)$ anymore and denote this model simply by ℓ_p .

Proposition 1.4. *The McClure-Staffeldt model $\tilde{\ell}_p$ of the p -complete connective Adams summand is equivalent as an E_∞ ring spectrum to ℓ_p .*

Remark 1.5. If E is a commutative \mathbb{S} -algebra with naive G -action for some group G , then neither the connective cover functor $\bar{c}(-)$ nor Bousfield localization of E has to commute with taking homotopy fixed points. As an example, consider connective complex K -theory ku with the conjugation action by C_2 . The homotopy fixed points ku^{hC_2} are not equivalent to ko , but on the periodic versions we obtain $KU^{hC_2} \simeq KO$.

Proof of Proposition 1.4. Consider the algebraic K -theory model for connective complex K -theory, $ku = K(\mathbf{k})$, with $\mathbf{k} = \bigcup_i \mathbb{F}_{q^{p^i(p-1)}}$. The canonical inclusions $\mathbb{F}_{q^{p^i}} \hookrightarrow \mathbb{F}_{q^{p^i(p-1)}}$ assemble into a map $j: \mathbf{k}' \rightarrow \mathbf{k}$. The Galois group C_{p-1} of \mathbf{k} over \mathbf{k}' acts on \mathbf{k} and induces an action on algebraic K -theory. As \mathbf{k}' is fixed under the action of C_{p-1} there is a factorization of $K(j)_p$ as

$$\begin{array}{ccc} K(\mathbf{k}')_p & \xrightarrow{K(j)_p} & K(\mathbf{k})_p \\ & \searrow i & \nearrow \\ & K(\mathbf{k})_p^{hC_{p-1}} & \end{array}$$

and i yields a weak equivalence of commutative \mathbb{S} -algebras, where $K(\mathbf{k})_p^{hC_{p-1}}$ is a model for the connective p -complete Adams summand which is weakly equivalent to ℓ_p by construction.

Consider the composition of the following chain of maps between commutative \mathbb{S} -algebras:

$$K(\mathbf{k}')_p \xrightarrow{i} (K(\mathbf{k})_p)^{hC_{p-1}} \longrightarrow K(\mathbf{k})_p \longrightarrow KU_p.$$

The target KU_p is as well the target of the map $\bar{c}(KU_p) \rightarrow KU_p$. Note that the universal property of $\bar{c}(-)$ yields a zigzag $\varsigma: K(\mathbf{k})_p \rightleftarrows \bar{c}(KU_p)$ of equivalences between $K(\mathbf{k})_p$ and $\bar{c}(KU_p)$.

As KU_p is the Bousfield localization of $K(\mathbf{k})_p$ in the category of $K(\mathbf{k})_p$ -modules with respect to the Bott element,

$$KU_p = L_{K(\mathbf{k})_p[\beta^{-1}]}^{K(\mathbf{k})_p} K(\mathbf{k})_p,$$

it inherits the C_{p-1} -action on $K(\mathbf{k})_p$. The functoriality of the connective cover lift this action to an action on $\bar{c}(KU_p)$.

The connective cover functor is in fact a functor in the category of commutative \mathbb{S} -algebras with naive G -action for any group G . We have to show that the map $\bar{c}(A) \rightarrow A$ is G -equivariant if A is a commutative \mathbb{S} -algebra with a naive G -spectrum underlying it. The functor $B(\mathbb{P}, \mathbb{P}, \mathbb{L})$ does not cause any problems. Proving the claim for the functor c involves chasing the definition given in [9, VII, §3].

The prespectrum underlying $c(A)$ applied to an inner product space V is $T(A_0)(V)$, where A_0 is the zeroth space of the spectrum A and T is a certain bar construction involving suspensions and a monad consisting of the product of a fixed E_∞ -operad with the partial operad of little convex bodies \mathcal{K} . For a fixed V the suspension Σ^V and the operadic term \mathcal{K}_V are used. As the G -action is compatible with the E_∞ and the additive structure of A , the evaluation map $(T(A_0)(V) \rightarrow A(V))$ is G -equivariant. For varying V , these maps constitute a map of prespectra and its adjoint on the level of spectra is $c(A) \rightarrow A$. As the spectrification functor preserves G -equivariance, the claim follows. Therefore the resulting zigzag $\varsigma: K(\mathbf{k})_p \rightleftarrows \bar{c}(KU_p)$ is C_{p-1} -equivariant and we obtain an induced zigzag on homotopy fixed points,

$$\varsigma^{hC_{p-1}}: (K(\mathbf{k})_p)^{hC_{p-1}} \rightleftarrows (\bar{c}(KU_p))^{hC_{p-1}}.$$

As ς is an isomorphism in the homotopy category and is C_{p-1} -equivariant, $\varsigma^{hC_{p-1}}$ yields an isomorphism as well. \square

2. CONNECTIVE LUBIN-TATE SPECTRA

Goerss and Hopkins proved in [8] that the Lubin-Tate spectra E_n with

$$(E_n)_* = W(\mathbb{F}_{p^n})[[u_1, \dots, u_{n-1}]] [u^{\pm 1}] \quad \text{with } |u_i| = 0 \text{ and } |u| = -2$$

possess unique E_∞ structures for all primes p and all $n \geq 1$. The connective cover $c(E_n)$ has coefficients

$$(c(E_n))_* = W(\mathbb{F}_{p^n})[[u_1, \dots, u_{n-1}]] [u^{-1}] \quad \text{with } |u_i| = 0 \text{ and } |u| = -2.$$

Of course $\bar{c}(E_n)[(u^{-1})^{-1}] \sim E_n$.

The spectra $BP\langle n \rangle$ can be built from the Brown-Peterson spectrum BP by killing all generators of the form v_m with $m > n$ in $BP_* = \mathbb{Z}_{(p)}[v_1, v_2, \dots]$. Using for instance Angeltveit's result [1, theorem 4.2] one can prove that the $BP\langle n \rangle$ are A_∞ spectra and from [4] it is known that this \mathbb{S} -algebra structure can be improved to an MU -algebra structure. On the other hand, Strickland showed in [13] that $BP\langle n \rangle$ with $n \geq 2$ is not a homotopy commutative MU -ring spectrum for $p = 2$. We offer $c(E_n)$ as a replacement for the p -completion $BP\langle n \rangle_p$ of $BP\langle n \rangle$.

We also need to recall that in the category of MU -modules, $E(n)$ is the Bousfield localization of $BP\langle n \rangle$ with respect to $BP\langle n \rangle[v_n^{-1}]$, hence by [7] it inherits the structure of an MU -algebra and the natural map $BP\langle n \rangle \rightarrow E(n)$ is a morphism of MU -algebras. Furthermore, the Bousfield localization of $E(n)$ with respect to the MU -algebra $K(n)$ is the I_n -adic completion $\widehat{E(n)}$, which was shown to be a commutative \mathbb{S} -algebra in [5], and the natural map $\widehat{E(n)} \rightarrow E_n$ is a morphism of commutative \mathbb{S} -algebras, see for example [6, example 2.2.6]. Thus there is a morphism of ring spectra $BP\langle n \rangle \rightarrow E_n$ which lifts to a map $BP\langle n \rangle \rightarrow c(E_n)$.

Proposition 2.1. $BP\langle n \rangle$ and $BP\langle n \rangle_p$ are Bousfield equivalent to $c(E_n)$.

Proof. On coefficients, we obtain a ring homomorphism $(BP\langle n \rangle_p)_* \rightarrow (c(E_n))_*$ which on homotopy is given by

$$v_k \mapsto \begin{cases} u^{1-p^k} u_k & \text{for } 1 \leq k \leq n-1, \\ u^{1-p^n} & \text{for } k = n. \end{cases}$$

extending the natural inclusion of the p -adic integers $\mathbb{Z}_p = W(\mathbb{F}_p)$ into $W(\mathbb{F}_{p^n})$. This homomorphism is induced by a map of ring spectra.

Recall from [3] that $E(n)$ and $\widehat{E(n)}$ are Bousfield equivalent as \mathbb{S} -modules, and it follows that E_n is Bousfield equivalent to these since it is a finite wedge of suspensions of $\widehat{E(n)}$.

If X is a p -local spectrum with torsion free homotopy groups then its p -completion X_p is Bousfield equivalent to X , i.e., $\langle X_p \rangle = \langle X \rangle$. This follows using the cofibre triangles (in which $M(p)$ is the mod p Moore spectrum and the circled arrow indicates a map of degree one)

$$\begin{array}{ccc} X & \xrightarrow{p} & X \\ & \circlearrowleft & \searrow \\ & & X \wedge M(p) \end{array} \quad \begin{array}{ccc} X_p & \xrightarrow{p} & X_p \\ & \circlearrowleft & \searrow \\ & & X \wedge M(p) \end{array}$$

together with the fact that the rationalization $p^{-1}X$ is a retract of $p^{-1}(X_p)$. In particular, we have $\langle BP\langle n \rangle_p \rangle = \langle BP\langle n \rangle \rangle$ and $\langle E(n)_p \rangle = \langle E(n) \rangle$.

From [11, theorem 2.1], the Bousfield class of $BP\langle n \rangle$ is

$$\langle BP\langle n \rangle \rangle = \langle E(n) \rangle \vee \langle H\mathbb{F}_p \rangle.$$

There is a cofibre triangles

$$\begin{array}{ccc} \Sigma^2 c(E_n) & \xrightarrow{u^{-1}} & c(E_n) \\ & \circlearrowleft & \searrow \\ & & HW(\mathbb{F}_{p^n})[[u_1, \dots, u_{n-1}]] \end{array}$$

in which $HW(\mathbb{F}_{p^n})[[u_1, \dots, u_{n-1}]]$ is the Eilenberg-MacLane spectrum on $W(\mathbb{F}_{p^n})[[u_1, \dots, u_{n-1}]]$.

More generally we can construct a family of Eilenberg-MacLane spectra with coefficients $W(\mathbb{F}_{p^n})[[u_1, \dots, u_k]]$ for $k = 0, \dots, n-1$ which are related by cofibre triangles

$$\begin{array}{ccc} HW(\mathbb{F}_{p^n})[[u_1, \dots, u_k]] & \xrightarrow{u_k} & HW(\mathbb{F}_{p^n})[[u_1, \dots, u_k]] \\ & \circlearrowleft & \searrow \\ & & HW(\mathbb{F}_{p^n})[[u_1, \dots, u_{k-1}]] \end{array}$$

such that for $k = 0$ we obtain $HW(\mathbb{F}_{p^n})$. With the help of these cofibre sequences we can identify

$$\langle HW(\mathbb{F}_{p^n})[[u_1, \dots, u_k]] \rangle = \langle HW(\mathbb{F}_{p^n})[[u_1, \dots, u_{k-1}]] \rangle \vee \langle HW(\mathbb{F}_{p^n})[[u_1, \dots, u_k]][u_k^{-1}] \rangle.$$

In general, if R is a commutative ring, then the ring of finite tailed Laurent series $R((x))$ is faithfully flat over R and therefore we have

$$\langle HR((x)) \rangle = \langle HR \rangle.$$

Using this auxiliary fact we inductively get that

$$\langle HW(\mathbb{F}_{p^n})[[u_1, \dots, u_k]] \rangle = \langle HW(\mathbb{F}_{p^n})[[u_1, \dots, u_{k-1}]] \rangle.$$

This reduces the Bousfield class of $c(E_n)$ to $\langle E_n \rangle \vee \langle HW(\mathbb{F}_{p^n}) \rangle$. As $W(\mathbb{F}_{p^n})$ is a finitely generated free \mathbb{Z}_p -module and as $\langle H\mathbb{Z}_p \rangle = \langle H\mathbb{Q} \rangle \vee \langle H\mathbb{F}_p \rangle$ this leads to

$$\begin{aligned} \langle c(E_n) \rangle &= \langle E(n) \vee H\mathbb{Q} \vee H\mathbb{F}_p \rangle \\ &= \langle E(n) \vee H\mathbb{F}_p \rangle = \langle BP\langle n \rangle \rangle. \end{aligned} \quad \square$$

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